

The pressure at the bottom of a hydrostatic column of atmosphere can be found by integrating the hypsometric equation such that,

$$\begin{aligned} p(z_b) &= p(z_t) \exp\left(\frac{g}{R} \int_{z_b}^{z_t} T_v^{-1} dz\right) \\ &= p(z_t) \exp\left(\frac{g \Delta z}{R \overline{T}_v}\right), \end{aligned} \quad (1)$$

where  $z_t$  and  $z_b$  are the heights of the top and bottom

of the column, respectively,  $\Delta z = z_t - z_b$ , and  $\overline{T}_v$  is the mean virtual temperature in the column  $\Delta z$ . A similar expression for the height at some pressure level  $p_b$  is

$$\begin{aligned}
 z(p_b) &= z(p_t) + \frac{R}{g} \int_{p_b}^{p_t} T_v d \ln p \\
 &= z(p_t) + \frac{R\overline{T}_v}{g} \ln \left( \frac{p_t}{p_b} \right), \quad (2)
 \end{aligned}$$

where  $p_t$  is a pressure level at which the height is known. Equations (1) and (2) show that if  $p(z_t)$  and  $z(p_t)$  are fixed, then  $p(z_b)$  and  $z(p_b)$  decrease in magnitude as the mean temperature in the column increases. Thus, relative pressure and height minima / maxima on some height or pressure level, respectively, must lie below relatively warm / cold columns of air.